



# Geomechanics

## Critical State Material Models

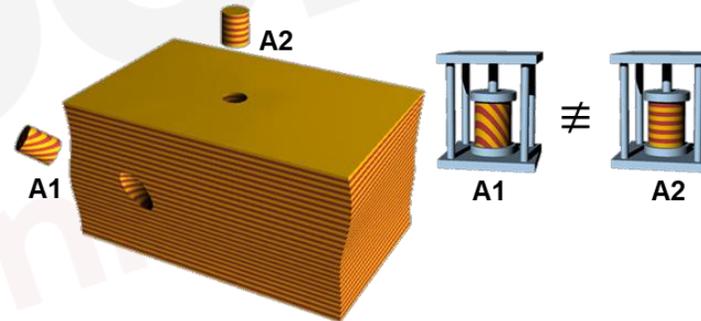
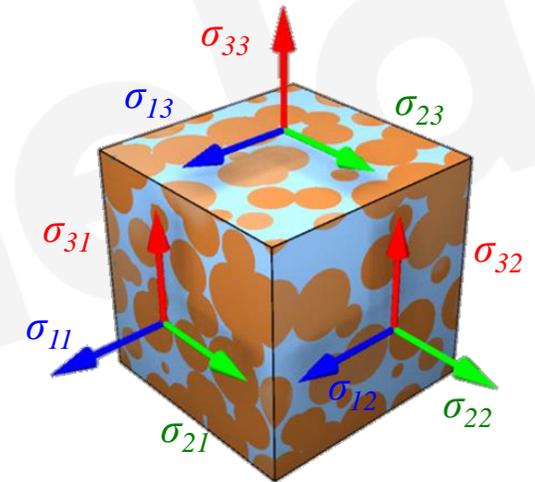
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### Introduction to Stress and Strain in Geomaterials

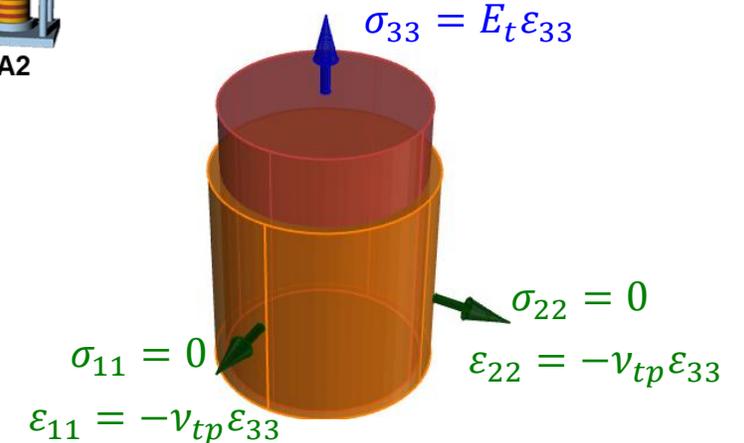
Within this section you will be guided through:

- Stress/strain components and invariants
- Elasticity – Young’s modulus and Poisson’s ratio, anisotropy
- Poroelasticity (pore pressure and mechanical interaction)
- Elastoplastic models; how they work



$$\begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{23} \\ \sigma_{13} \\ \sigma_{12} \end{bmatrix} = \frac{E}{(1+\nu)(1-2\nu)} \begin{bmatrix} 1-\nu & \nu & \nu & 0 & 0 & 0 \\ 1-\nu & \nu & \nu & 0 & 0 & 0 \\ \nu & \nu & 1-\nu & 0 & 0 & 0 \\ (1-2\nu)/2 & 0 & 0 & (1-2\nu)/2 & 0 & 0 \\ 0 & 0 & 0 & 0 & (1-2\nu)/2 & 0 \\ 0 & 0 & 0 & 0 & 0 & (1-2\nu)/2 \end{bmatrix} \begin{bmatrix} \varepsilon_{11} \\ \varepsilon_{22} \\ \varepsilon_{33} \\ 2\varepsilon_{23} \\ 2\varepsilon_{13} \\ 2\varepsilon_{12} \end{bmatrix}$$

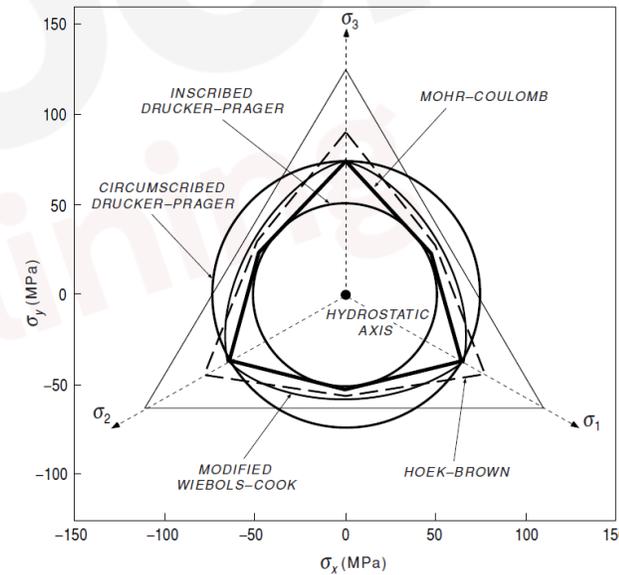
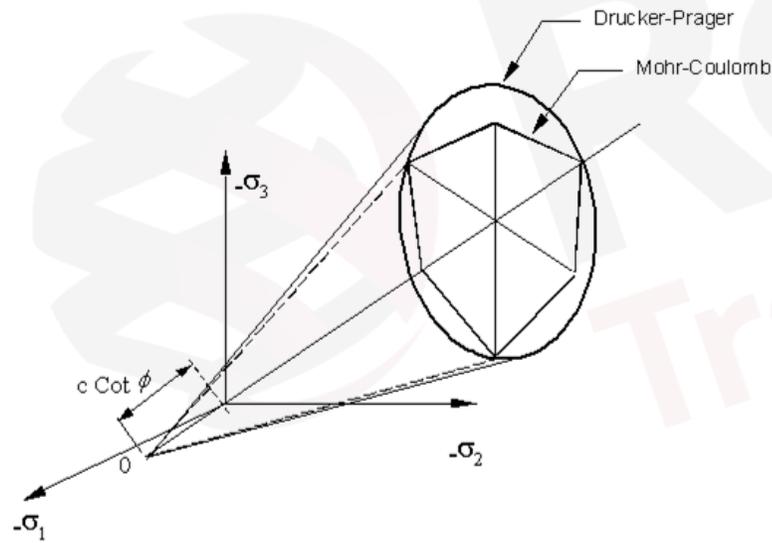
symm



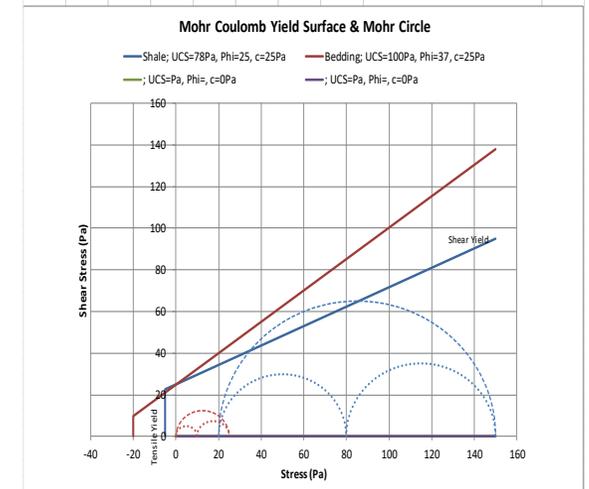
### Conventional Models and Extension to Critical State

Within this section you will be guided through:

- Brief description of critical state and non-critical state
- Mohr Coulomb, Drucker Prager, Modified Lade – description and examples
- Limitations of non-critical state models



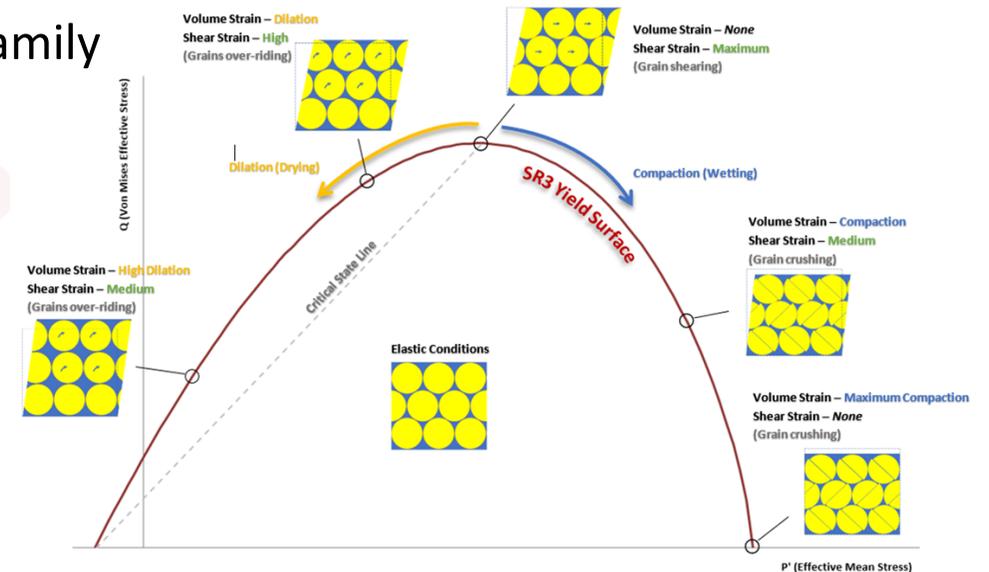
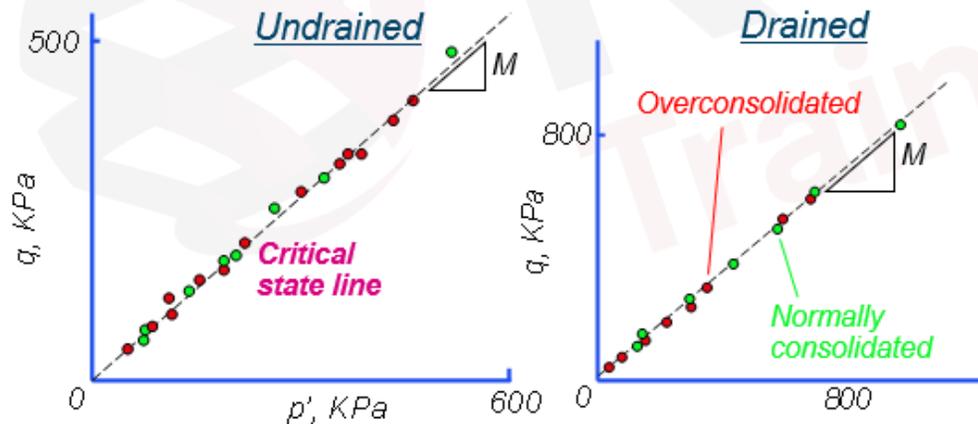
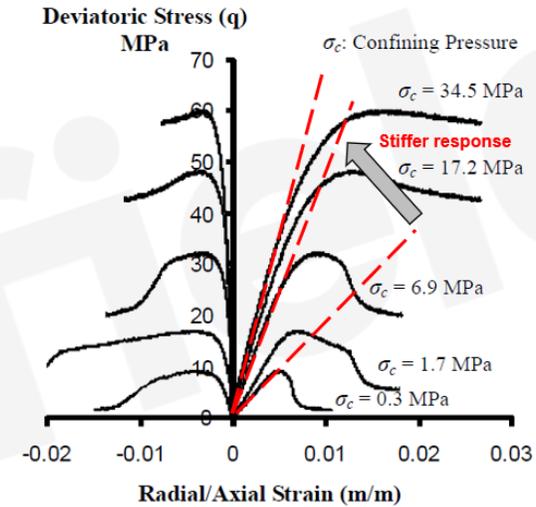
Units:		Pa									
Name	Input			Calc	Input			Legend			
	UCS	Phi	Tensile	c	Min Strs	Int Strs	Max Strs				
Shale	78	25	5	25	20	80	150	Shale: UCS=78Pa, Phi=25, c=25Pa			
Bedding	100	37	20	25	0	10	25	Bedding: UCS=100Pa, Phi=37, c=25Pa			
				0				; UCS=Pa, Phi=, c=0Pa			
				0				; UCS=Pa, Phi=, c=0Pa			



### Critical State Material Models

Within this section you will be guided through:

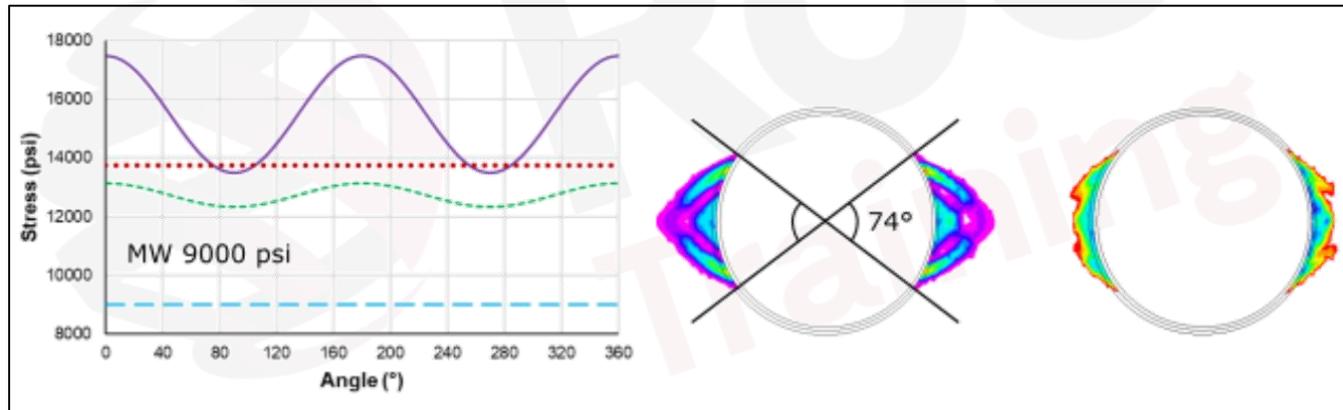
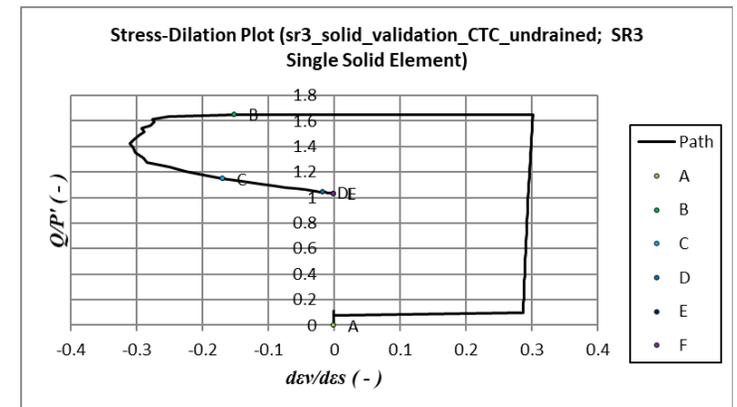
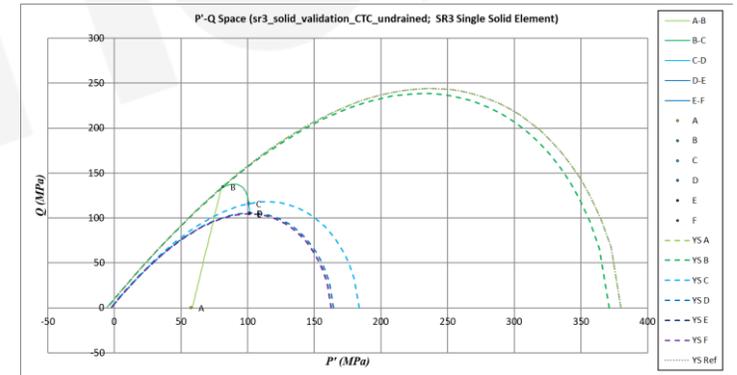
- Introduction to Critical State
- Experimental observations
- The Modified Cam Clay (MCC) model
- Extending MCC; an introduction to the SR3 model
- Advanced constitutive modelling – extended SR3 family



### Exercises

Although participants will be provided exercises throughout the course, specific examples include:

- Elfen wellbore – demonstration of elastic, perfectly plastic and shear softening
- Stress path assessments for typical material responses
- Material characterisations from lab tests



## Field Examples

To conclude the course, participants will be introduced to field examples where critical state and advanced constitutive behaviours are observed

- Wellbore stability – rupture modes, influence of bedding/anisotropy
- Shale creep – activating shale to form well barriers
- Reservoir stress paths and permeability evolution
- Sanding failure modes

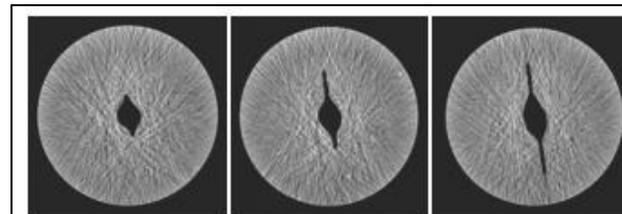
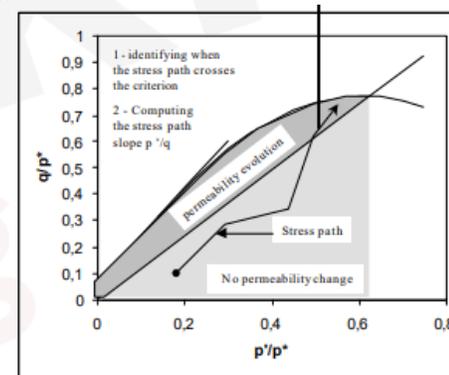
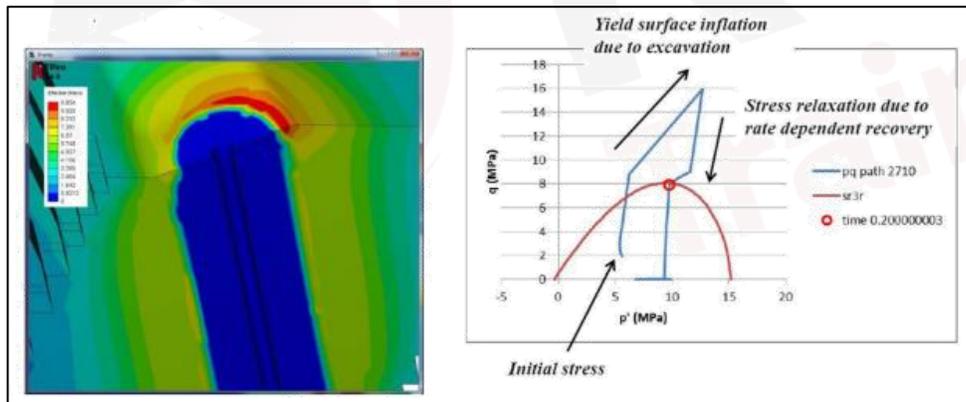
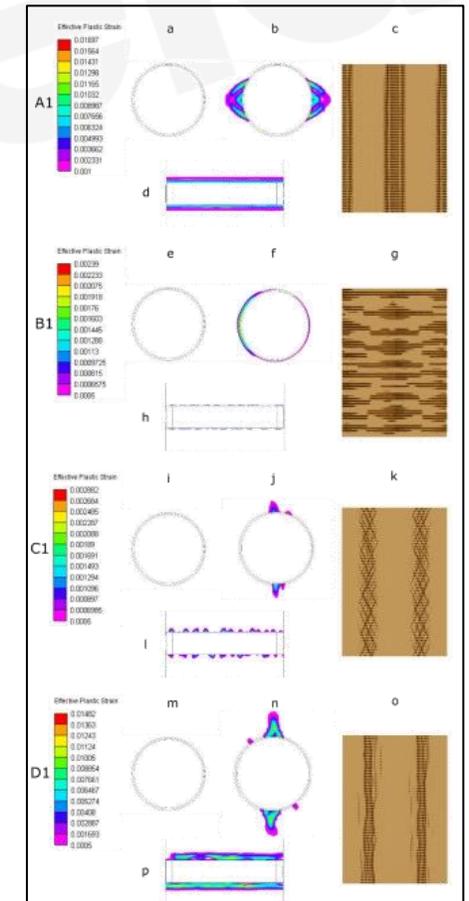


Figure 4. Various states of development of Class A slit failure in Castlegate sandstone.





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